

Digital Logic Design + Computer Architecture

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Instruction Set Architecture

How to talk to a Computer?

- **Computers can be given “instructions”**
- We have a set of instructions for every computer — called **instruction set**
- **When you write a program, you write instructions..**
 - More details later...
- Every instruction some hardware circuit implemented inside the processor to get its job done.
- **Instruction Set Architecture:** specifies the set of instructions a processor understands, their encoding, how they access memory etc...

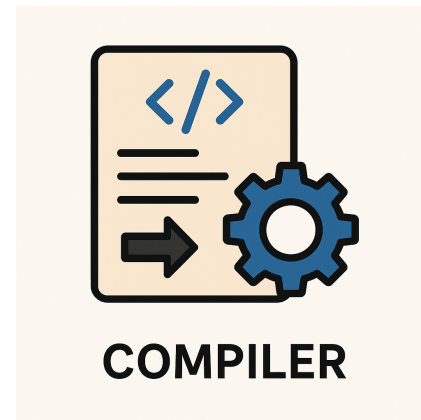


Image generated by ChatGPT

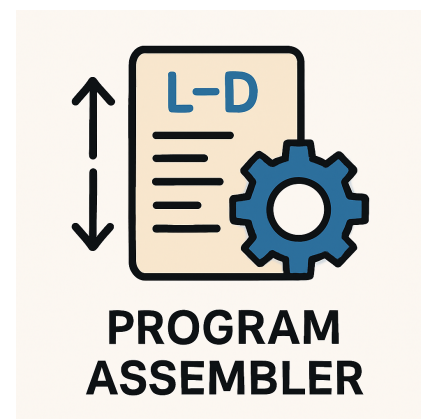
What happens when you write a program

- Say we write:

- $a = b + c;$



- There is a software program called **compiler**
 - Takes our code and encodes in terms of the instructions available for the computer
 - `add reg1, reg2, reg3`



- There is another program called **assembler** which converts the instruction (sequence) to bits
- 0101110000110101



Image generated by ChatGPT

How to talk to a Computer?

- **Instruction Set Architecture:** specifies the set of instructions a processor understands, their encoding, how they access memory etc...
 - **End of the day even your ChatGPT is a sequence of instructions** (many billions or trillions).
- Instruction set is basically an **abstraction layer**
 - **Hides the complexity of hardware from the software designers,**
 - **Interfaces the software and hardware.**



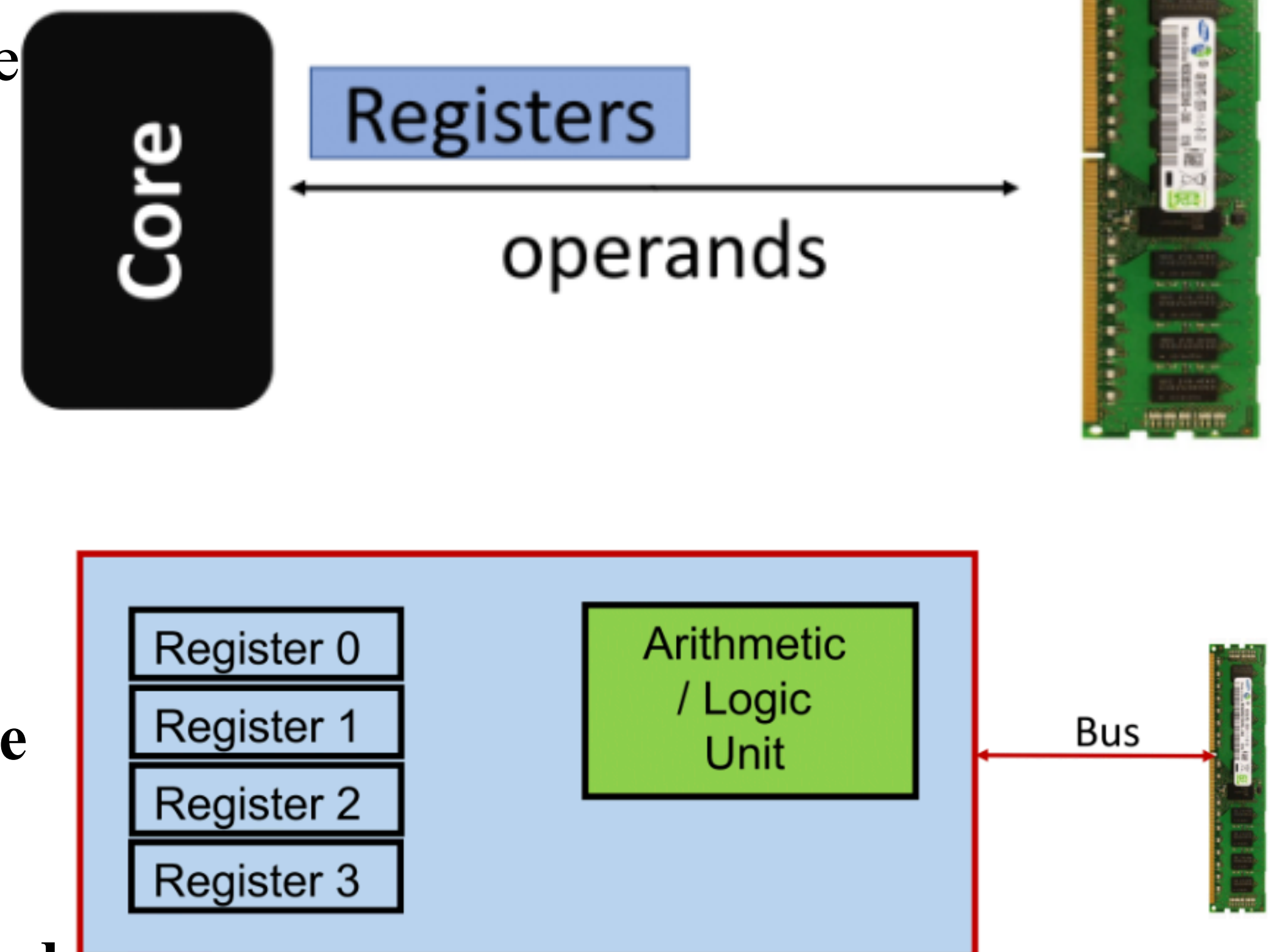
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Let's get into the processor a bit

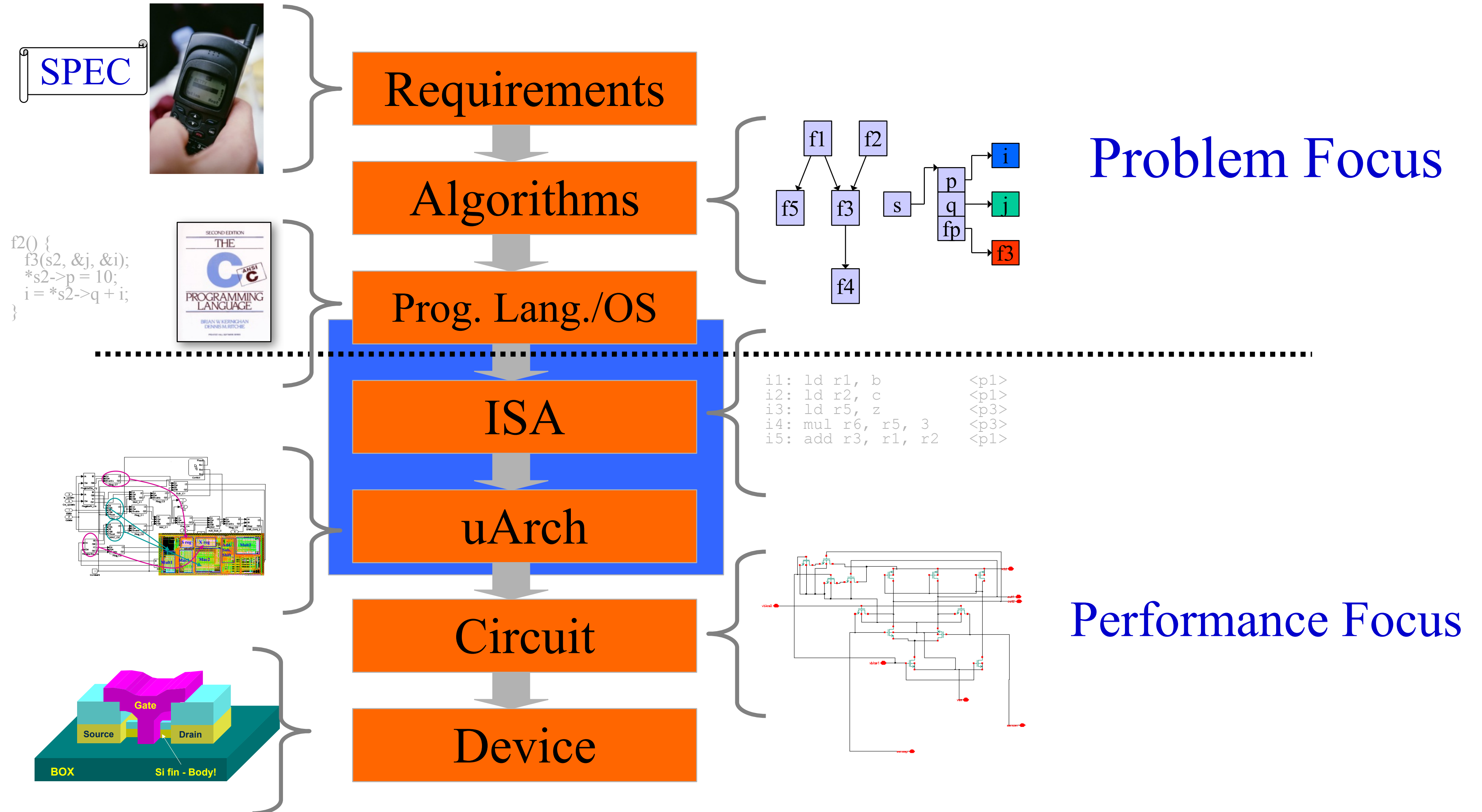
- It is a sequential circuit with a **limited** number of registers.
- It interacts with an external “memory”.
- Every instruction operates on some **operands** and generate results.

- Results and operands are stored in **registers**.
- **But they can also be in memory as the number of registers are limited**

- Note that typically such memory (called **DRAM** or **Dynamic Random Access Memory**) is off chip —outside the processor
- To operate, you have to bring the data from memory and store the results back

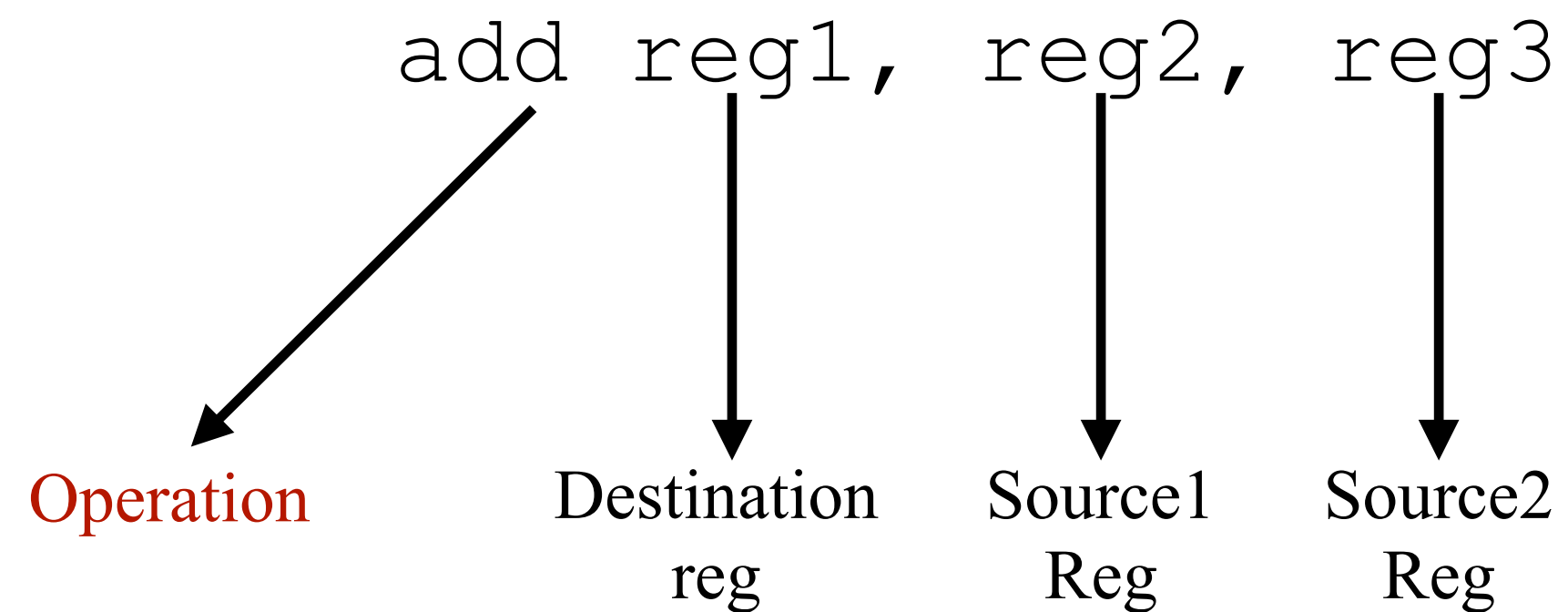


The Big Picture

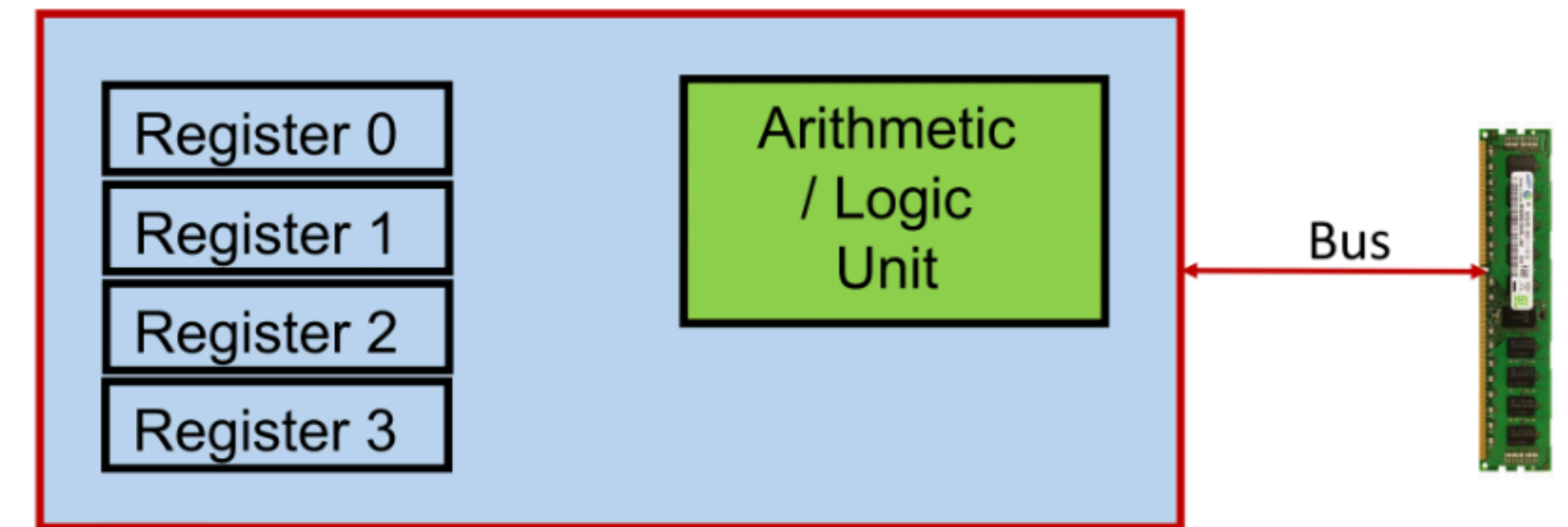


Dissection of an Instruction

- Let's focus on the simplistic view of the processor



- Most of the arithmetic/logical instructions can take this form — not all though



Instruction Set Architectures (ISA)

- There are many...
 - Intel uses **X86**
 - Apple uses a version of **AArch64** (ARM)
 - The entire world of embedded processors like ST-Microelectronics uses ARM
 - Now **RISC-V** is becoming a mainstream trend.
 - We shall study MIPS — a simple to understand ISA

Instruction Set Architectures (ISA)

- We shall study MIPS — a simple to understand ISA
 - Great for beginning...
 - Similar to ARM
 - Still in use in the embedded devices
 - Your smart card
 - Modems
 - Bitcoin-wallets

Now let's write some MIPS

- We shall name the registers as \$0, \$1, or \$a0, \$g1 etc...
- Now we shall try something a bit more complex...

add reg1, reg2, reg3



add \$0, \$1, \$2

Now let's write some MIPS

- Let's compute: $a = b + c - d$
- No idea? — get idea :P

add reg1, reg2, reg3



add \$0, \$1, \$2

Now let's write some MIPS

- Let's compute: $a = b + c - d$
- Assume we have add and sub instructions taking two sources and one destination register

```
add $0, $1, $2
```

```
sub $0, $1, $2
```


Now let's write some MIPS

- Let's compute: $a = b + c - d$
- Assume we have add and sub instructions taking two sources and one destination register

`add $0, $1, $2`

`sub $0, $1, $2`

- First' let's simplify :

• **Observe:** I use a temporary register...

- $t = b + c$
- $a = t - d$

- Now, I can map to instructions..

- `add $r0, $r1, $r2 // $t = b + c$`
- `sub $d0, $r0, $r3 // $a = t - d$`

Now let's write some MIPS

- Let's try: $f = (g+h) - (i+j)$

Now let's write some MIPS

- Let's try: $f = (g+h) - (i+j)$
 - `add $r0, $r1, $r2 // x = g+h`
 - `add $r3, $r4, $r5 // y = i+j`
 - `Sub $r0, $r0, $r3 // f = x-y`

- **Food of thought:** Well, do I really need to reuse registers???



Ok...A Few MIPS Details...

- We have 32 registers in the processor
 - So we have to reuse registers, no other option...
 - Typically, registers are 32-bits...
- But why don't we have infinite number of registers
 - Well, every piece of register is a real hardware...

• **But: Why 32??**



Ok...A Few MIPS Details...



- We have 32 registers in the processor
 - So we have to reuse registers, no other option...
 - Typically, registers are 32-bits...
 - Each instruction also encoded in 32 bits

• **But: Why 32??**

- But why don't we have infinite number of registers
 - Well, every piece of register is a real hardware...

The choice depends on several factors, like the speed of the execution, the usage and size of memory, the size of code, the encoding and decoding of instructions....**It's not a random choice...**

Immediate Instructions...

- $b = a + 7$

```
addi $r0, $r1, 7
```

- We don't need a register for the constant...
 - Can you tell me why?? Just guess...



Immediate Instructions...

- $b = a + 7$

`addi $r0, $r1, 7`

- We don't need a register for the constant...
 - Can you tell me why?? Just guess...



- `i` stands for 'immediate'
- The constant is in 2's complement form and of 16 bits.
- Question: Do I need a `subi` instruction??

Zero Is Very Special in Our Life...

- MIPS has a register which is called `$zero`
 - It stores 0
 - What is the purpose?
 - Well, a lot...you will see
 - A simple use of `$zero`

```
add $r1, $r0, $zero // a = b
```

- But again, why???



Zero Is Very Special in Our Life...

- MIPS has a register which is called `$zero`
 - It stores 0
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 - A simple use of `$zero`

```
add $r1, $r0, $zero // a = b
```

- But again, why??? — **just not needed**



a=b....The Pseudo-Instructions

- You can still write...

```
move $r1, $r0 // a = b
```

- But it is a pseudo-instruction
- Internally it converts to add
- Once again an engineering choice
- There are many such pseudo-instructions. See:

https://en.wikibooks.org/wiki/MIPS_Assembly/Pseudoinstructions

Logical Instructions

- Your good old Boolean algebra

sll, srl, and, or, nor, andi, ori etc

No **not** instruction 😊, well not is nor with one operand=0

- Remember: **These are bitwise operations...**
 - **Treats the operands as bit strings instead of numbers**

Logical Instructions

- Your good old Boolean algebra

sll, srl, and, or, nor, andi, ori etc

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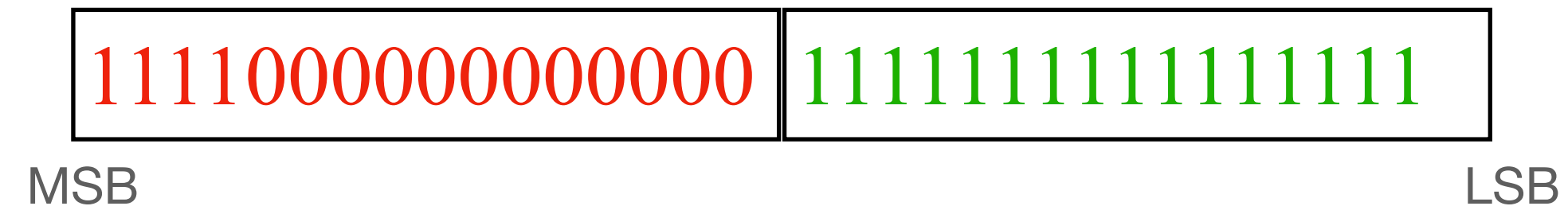
- Remember: **These are bitwise operations...**
 - **Treats the operands as bit strings instead of numbers**

Critical Thinking...

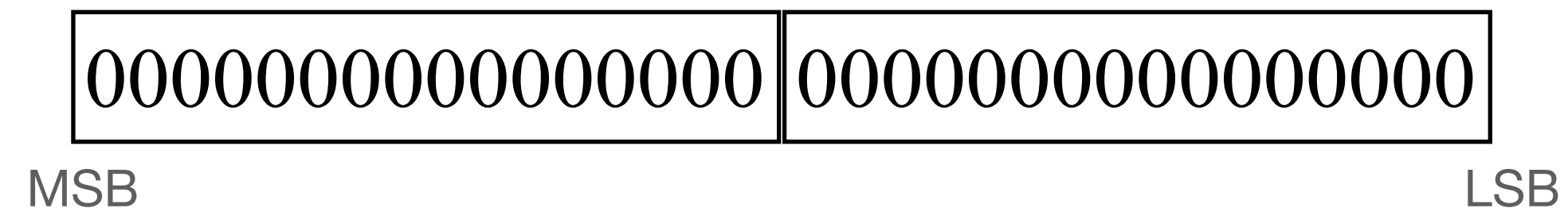
- We have seen that constants are 16 bits...
- But registers are 32-bits...
- How to store a 32-bit constant in a register???
- Let's say the constant is:
 - 11110000000000001111111111111111
 - In Hex: 0xF000FFFF
- **Info:** You have the following new instruction:
 - `lui $r0, const` // loads const in the upper 16 bits of the register \$r0

Critical Thinking...

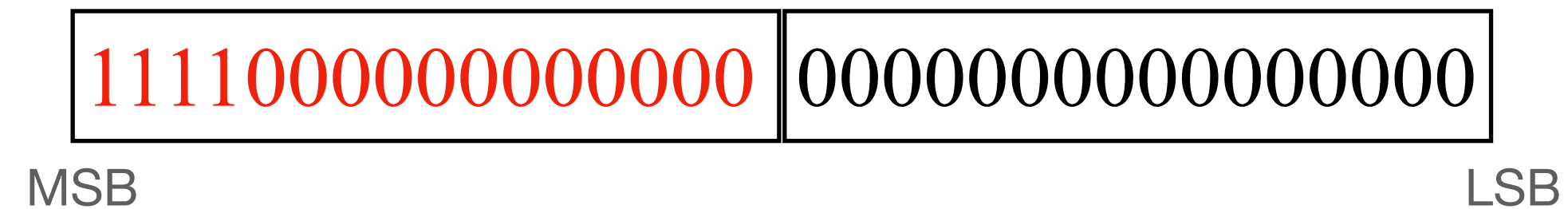
- Think, how the data will be represented inside your register...



- Initially The register `$r0` is at (simplifying assumption...does not matter)

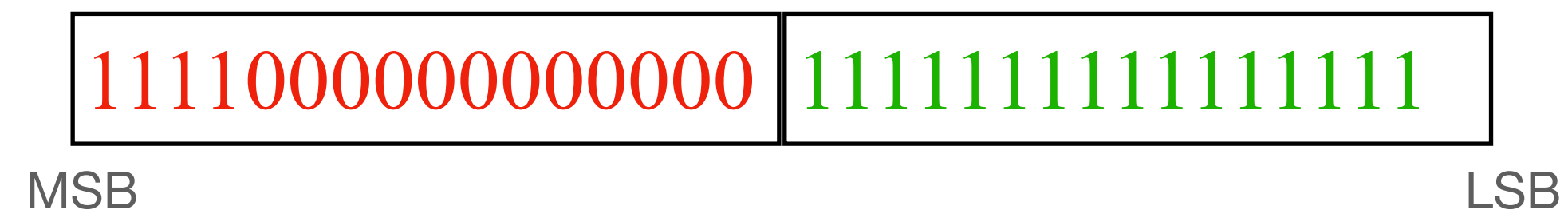


- Now do: `lui $r0, 0xF000`



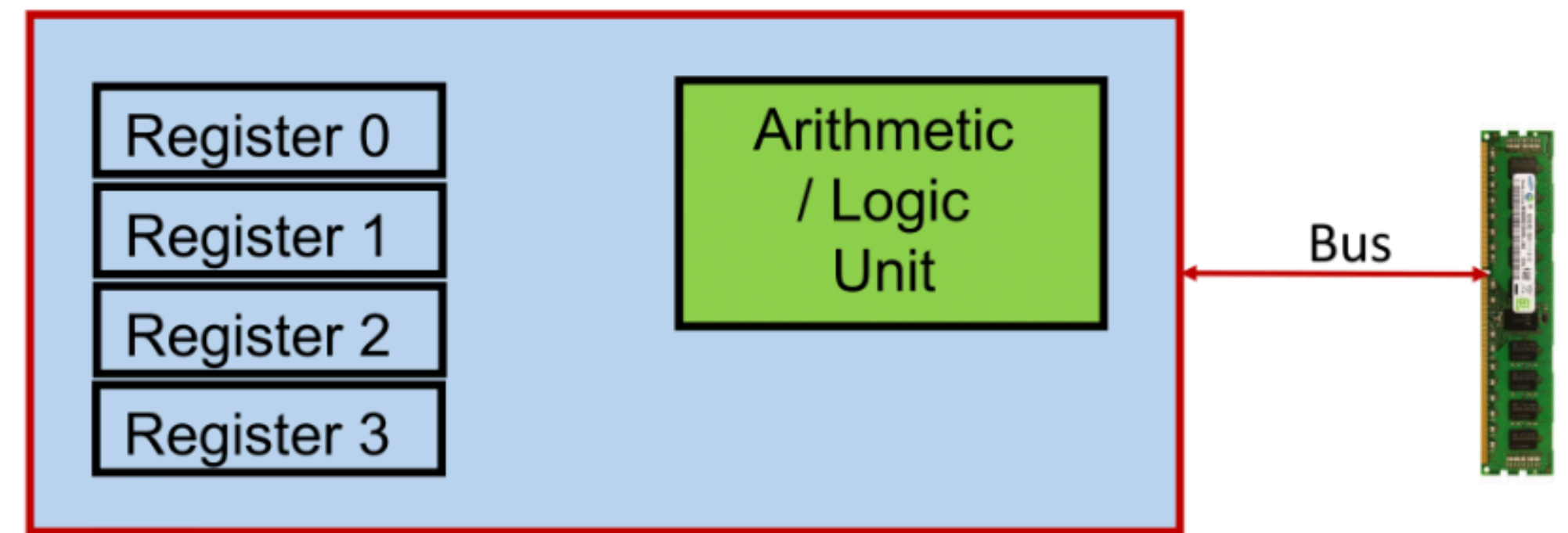
- Now do**, `addi $r0, 0xFFFF`

- You can also do `ori`



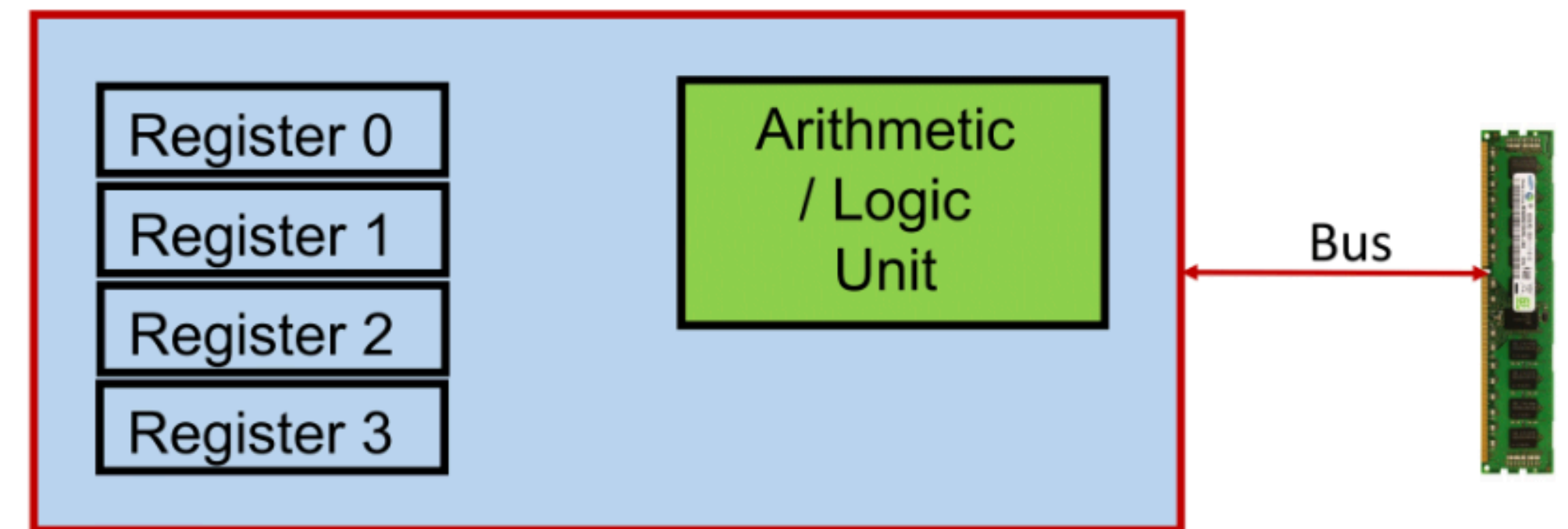
How to Use Your Memory??

- Recall, that MIPS only have 32 registers.
- Have you ever cared about counts while declaring variables in your program? — No way...
- Then how things work?
 - How can every program fits itself in 32 registers?



How to Use Your Memory??

- **Solution:**
 - Just store things in an external memory
 - Fetch the data to registers whenever it is required
 - Store the results after processing.
 - But still something is missing here...What is that??



How to Use Your Memory??

- Name this person?



How to Use Your Memory??

- Name this person?
 - John Luis von Neumann



How to Use Your Memory??

- In the old days, “programming” involved actually changing a machine’s physical configuration:
 - by flipping switches or connecting wires.
 - Memory only stored data that was being operated on.
- Then around 1944, **John von Neumann and others got the idea to encode instructions in a format that could be stored in memory just like data. — Stored program paradigm**
 - The processor interprets and executes instructions from memory



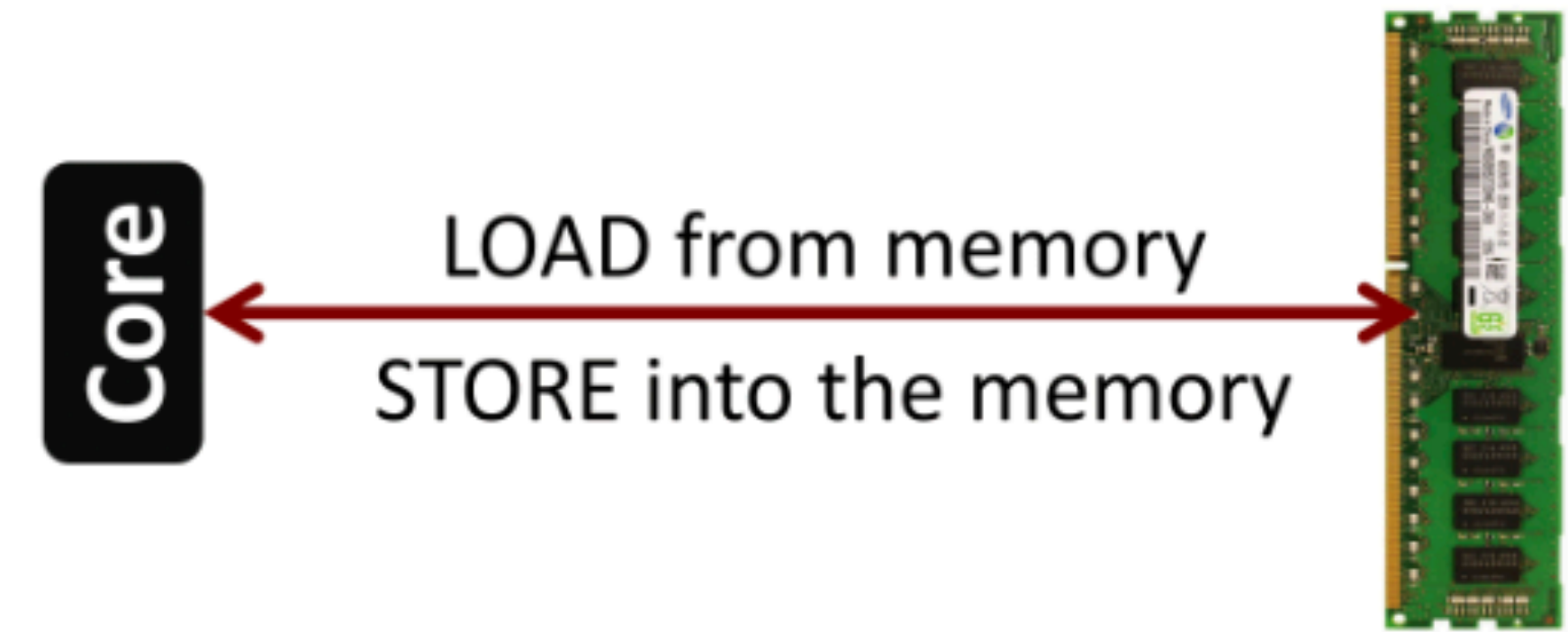
How to Use Your Memory??

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Memory Instructions

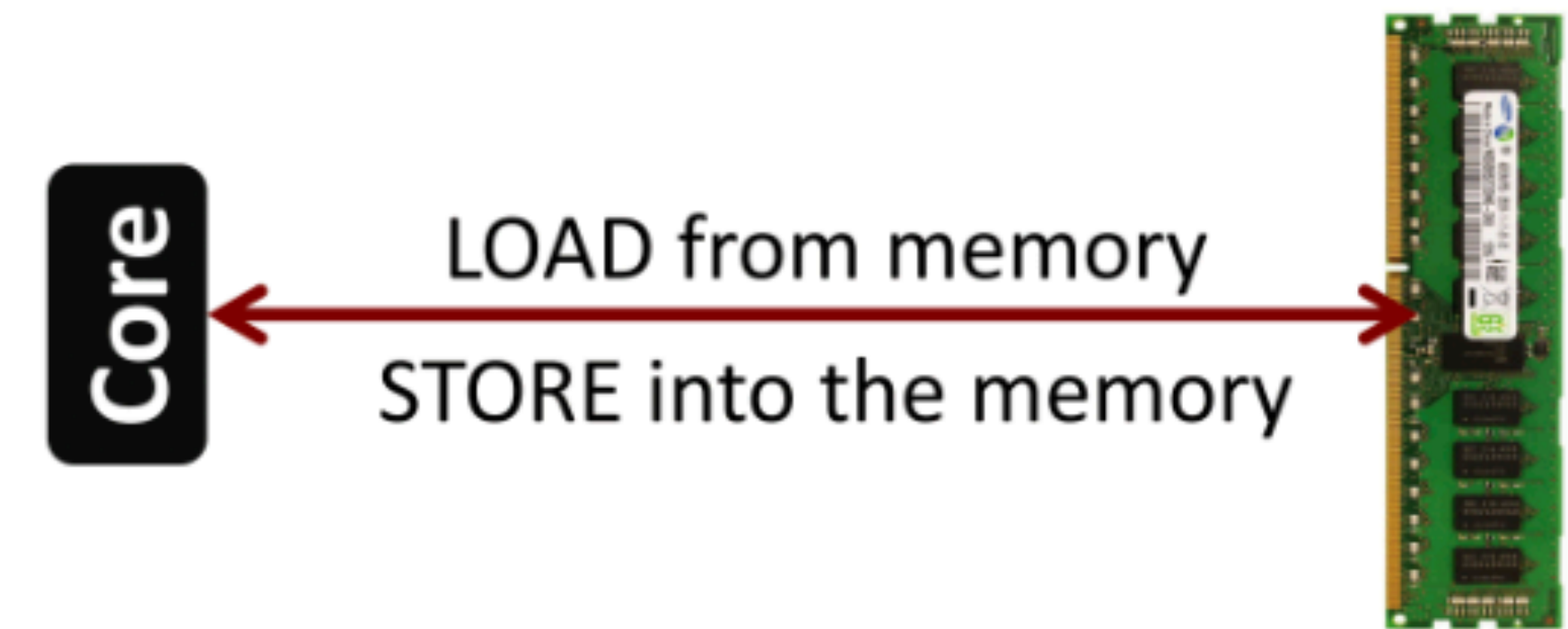
- **Load-Store Architecture:**
 - Load your data to process
 - Store it back...
- Instructions are handled in a slightly different manner....will come to that...



```
lw $t0, 1($a0)    # $t0 = Memory[$a0 + 1]  
sw $t0, 1($a0)    # Memory[$a0 + 1] = $t0
```


Memory Instructions

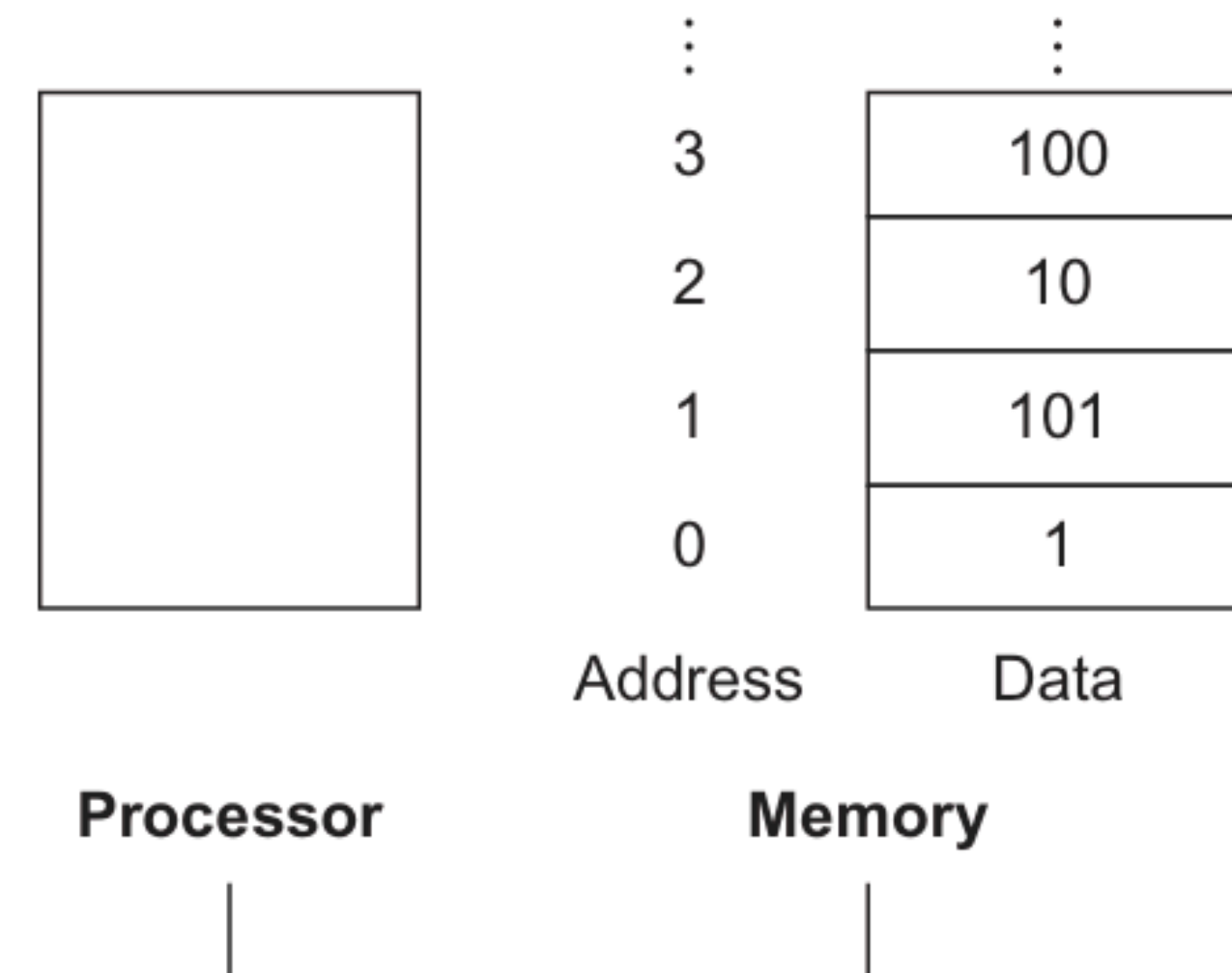
- **Load-Store Architecture:**
 - Load your data to process
 - Store it back...
- Instructions are handled in a slightly different manner....will come to that...
- **But, a critical question:**
 - How do you know where to find the data inside memory?



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Memory Instructions

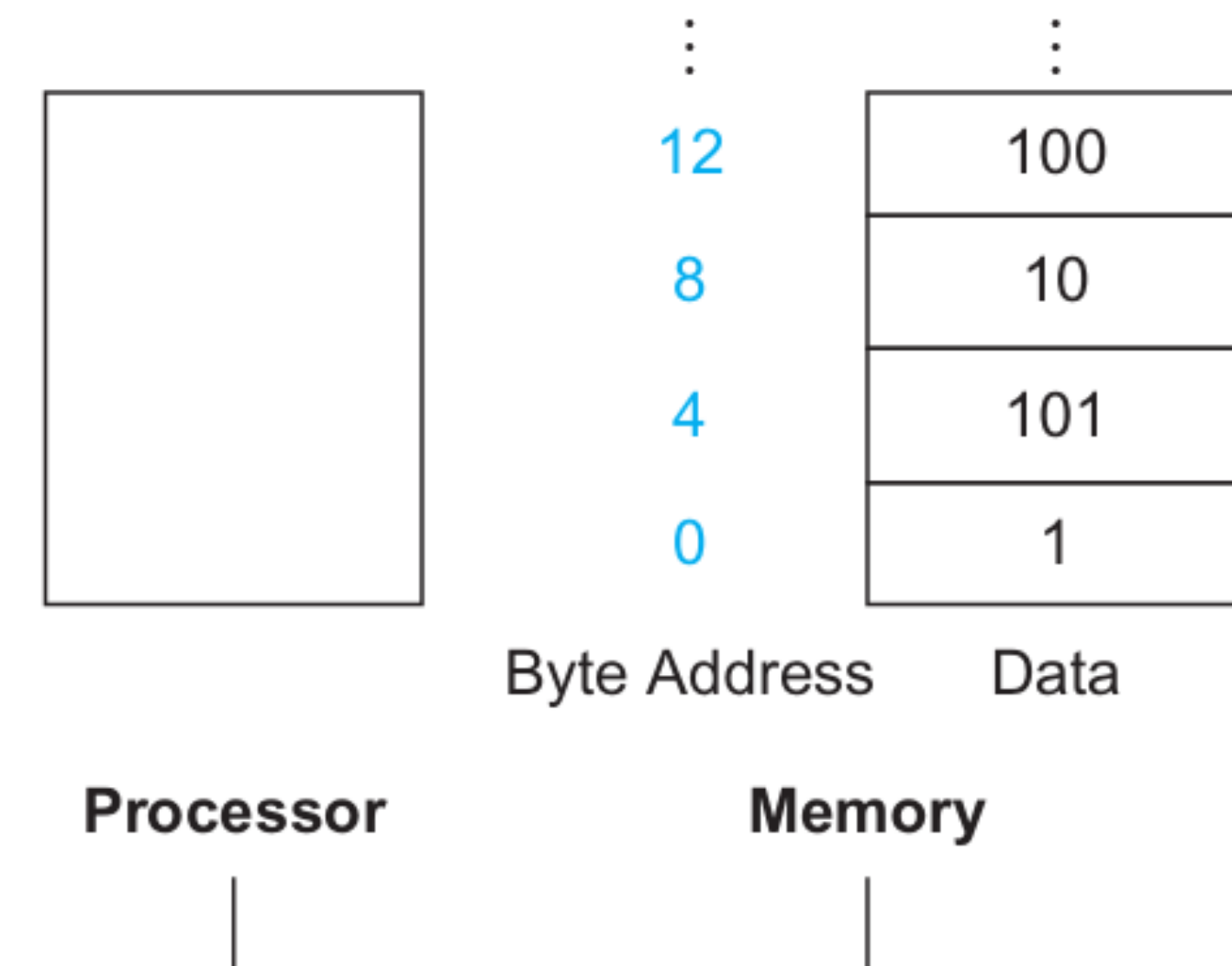
- But, a critical question:
 - How do you know where to find the data inside memory?
 - Memory has addresses
 - Think it like a large contiguous array...
 - **Every byte in memory has an unique address**
 - **Byte-addressable**
 - **BTW, each address is 32-bit in MIPS**



Memory Instructions

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lw $t0, 1($a0)    # $t0 = Memory[$a0 + 1]
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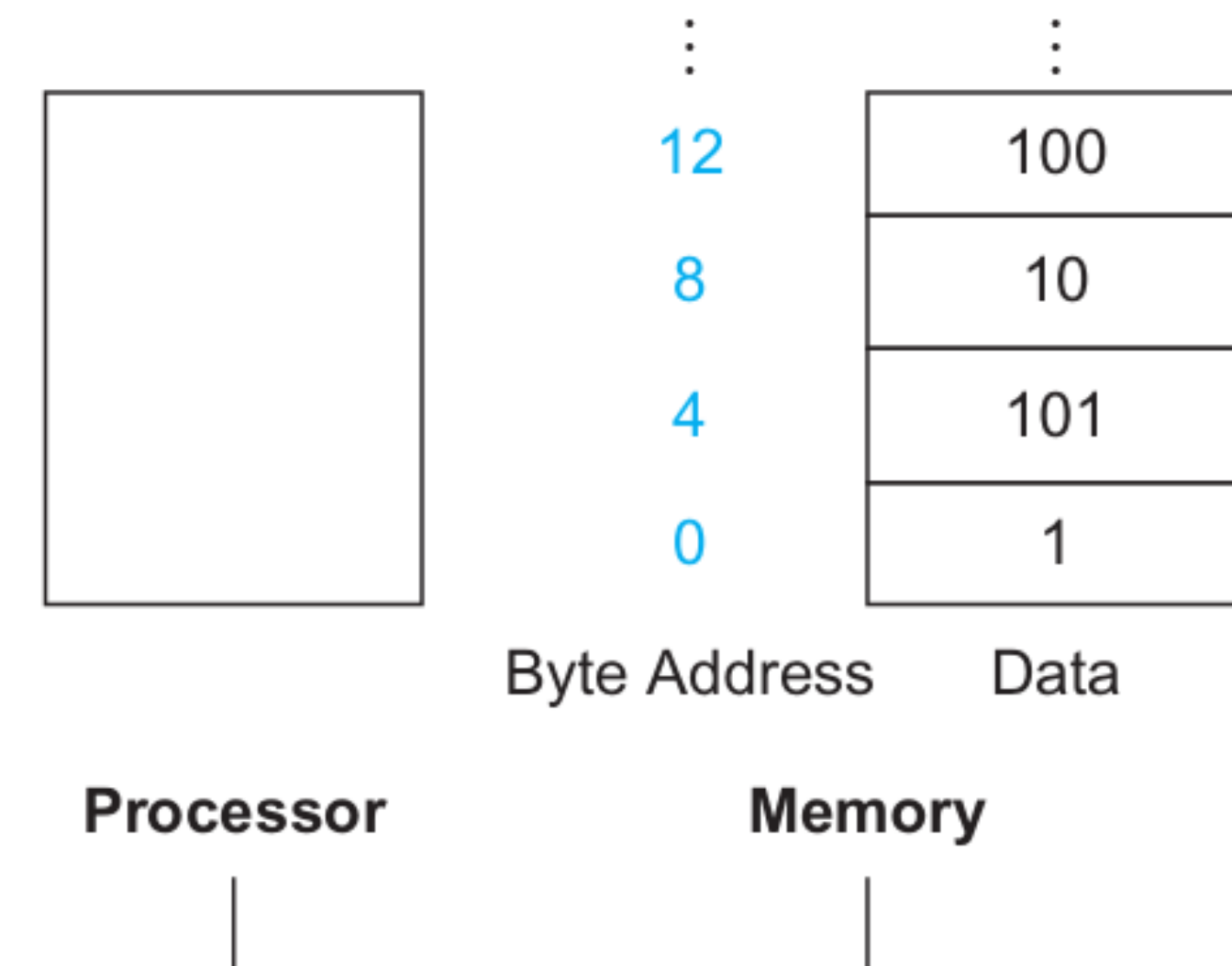
- The `lw` is interpreted as “load word”
 - MIPS also have other variants like “load byte” (`lb`)
- Data comes in `$t0`.
- But what is the `1($a0)` part signify?
 - `$a0` is the *base address* of the location you want to read from memory
 - `1` is called the *offset*.
- But why don't you read directly?



Memory Instructions

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lw $t0, 1($a0)    # $t0 = Memory[$a0 + 1]
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- But what is the `1($a0)` part signify?
 - `$a0` is the *base address* of the location you want to read from memory
 - `1` is called the *offset*.
- But why don't you read directly?
 - Again a design choice, to ease compilation, programming, and hardware design...

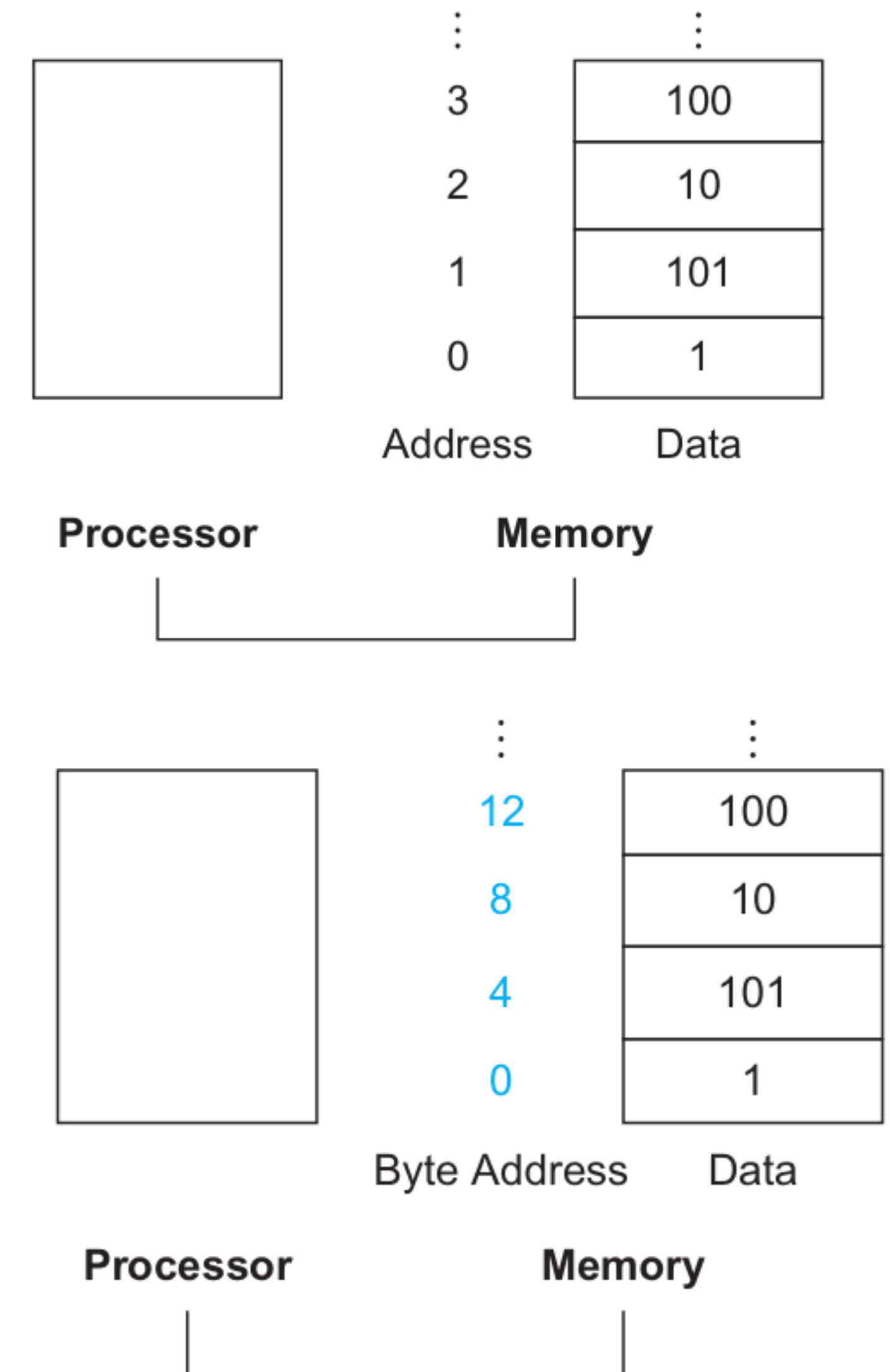


Memory Instructions: Word vs. Byte

`lw $t0, 1($s0)`

`lb $t0, 1($s0)`

- `lw` is interpreted as “**load word**”
- `lb` is “**load byte**”
- For the `lw`, we need the base+offset ($\$s0 + 1$) to be **always divisible by 4 — word alignment**
- Why?
- Nothing such for `lb`
- **What Lies Beneath?**
 - `lb` just read the byte in the calculated address
 - `lw` reads four consecutive bytes starting from the calculated address.
- Why word alignment — **again, it simplifies hardware OS, compiler....**

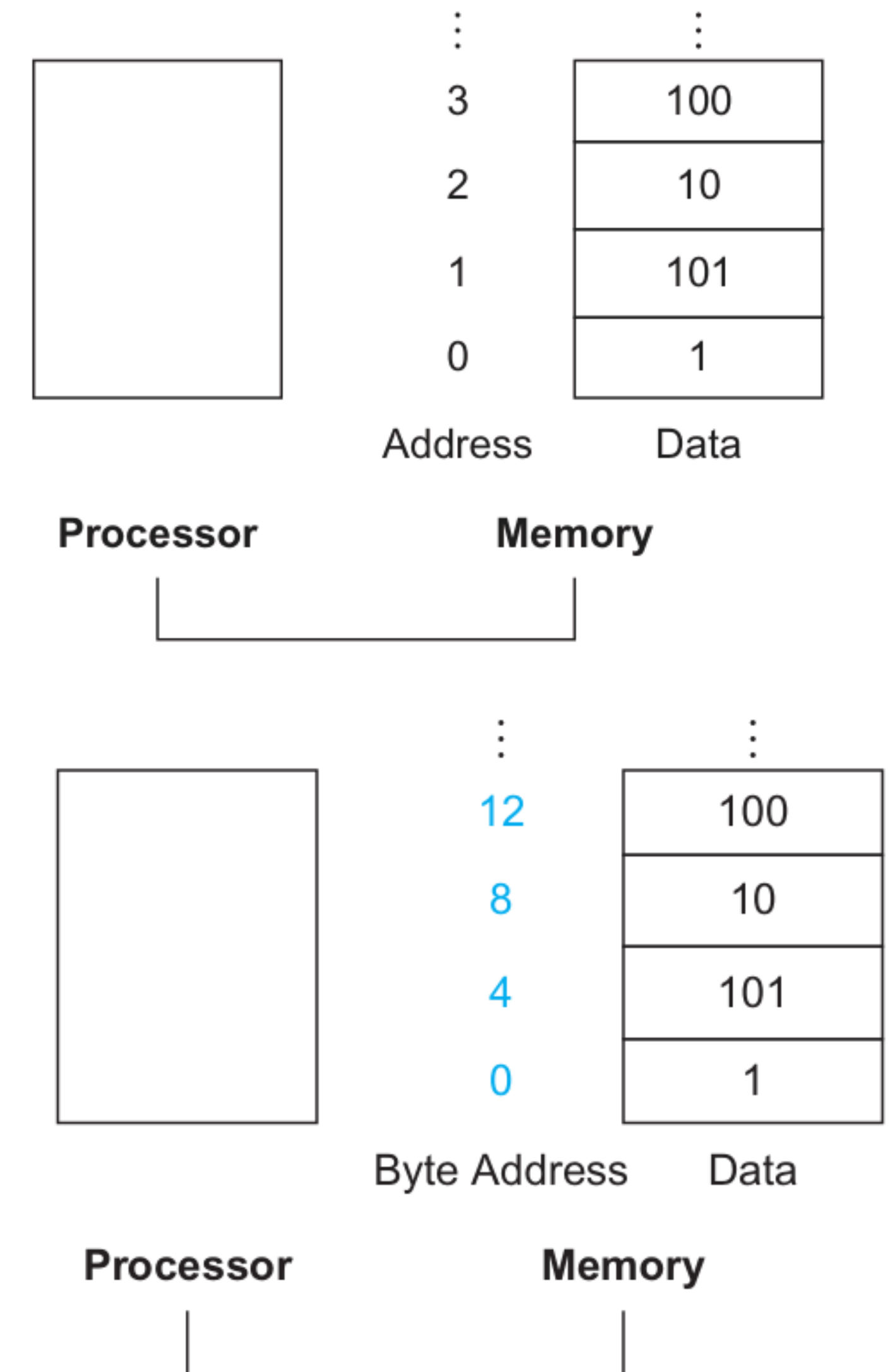


Memory Instructions: Word vs. Byte

`lw $t0, 1($s0)`

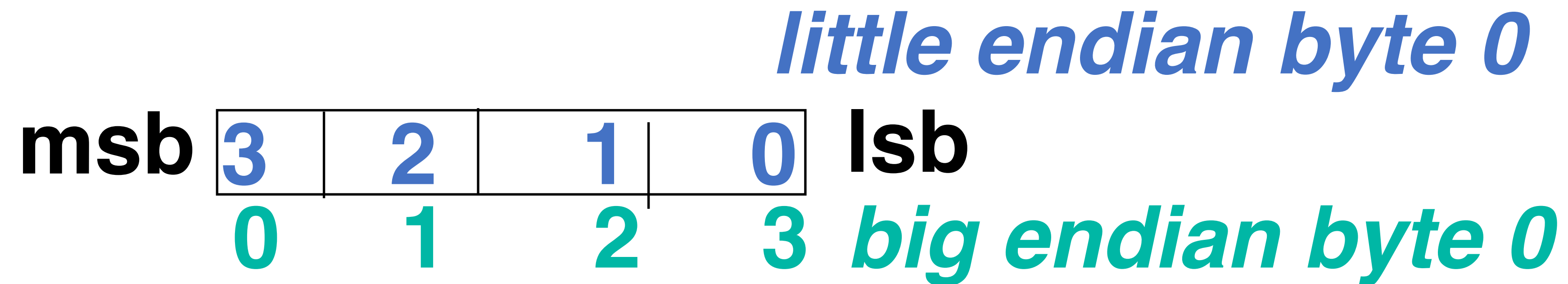
`lb $t0, 1($s0)`

- `lw` is interpreted as “load word”
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- Why?
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- **What Lies Beneath?**
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- Why word alignment — **again, it simplifies hardware OS, compiler....**



Endianness (Byte ordering within a word)

- **Big Endian:** address of most significant byte = word address
(**xx00** = Big end of word), MIPS
- **Little Endian:** address of least significant byte = word address
(**xx00** = Little end of word), x86



Just for an example, do not take it for granted ...

```
unsigned int i = 1;  
char *c = (char*)&i; // reading the LSB  
Printf ("%d", *c);
```

```
unsigned int i = 12345678;  
char *c = (char*)&i;  
Printf ("%d", *c);
```

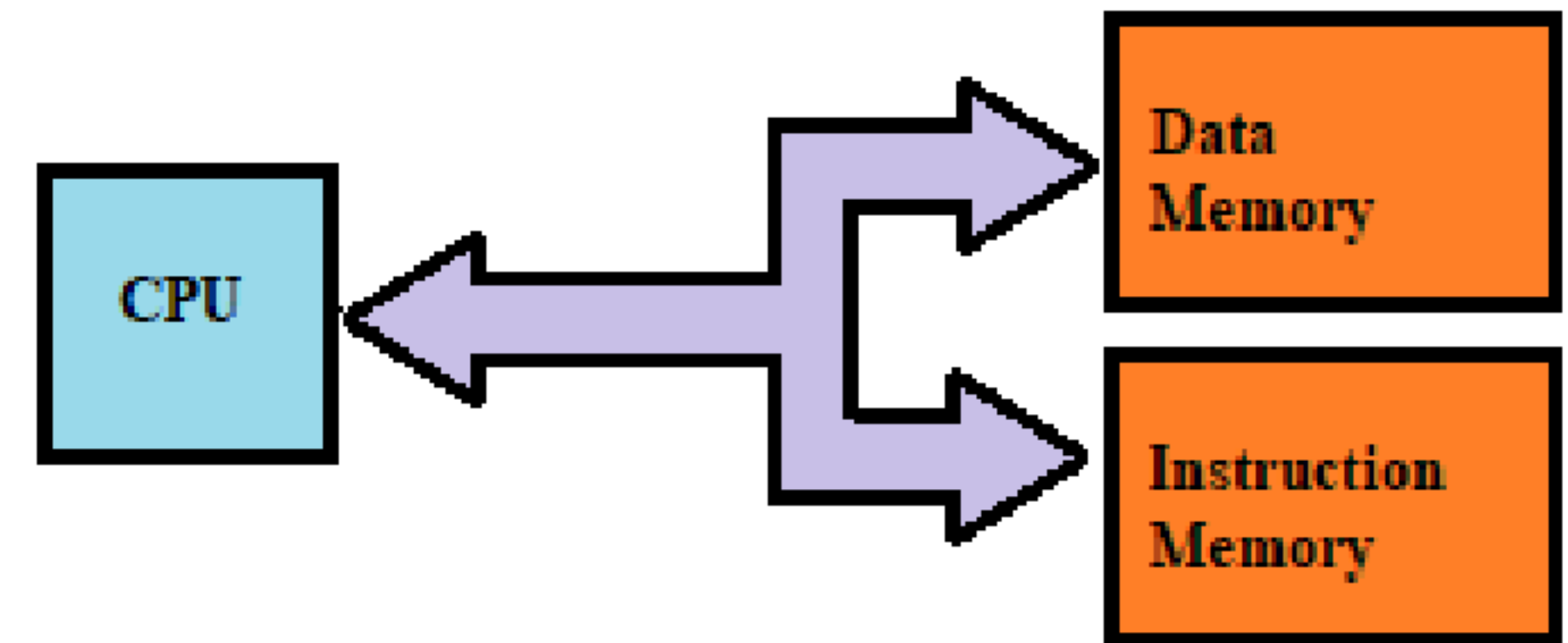


```
unsigned int i = 1;  
char *c = (char*)&i; // reading the LSB  
Printf ("%d", *c);  
Little endian: 1  
Big endian: 0
```

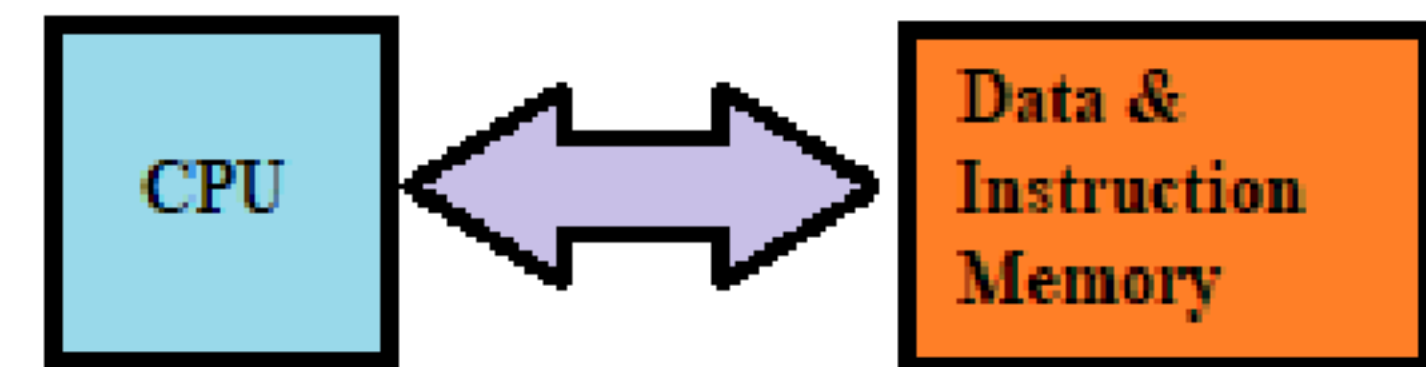
```
unsigned int i = 12345678;  
char *c = (char*)&i;  
Printf ("%d", *c);  
Little endian: 78  
Big endian: 12
```

Another Important Point...

- Ok, **Von Neumann** said, data and code both are stored in the same memory.
 - In practice, this may lead to an issue — at a specific interval of time, **you can either fetch a data or an instruction.**
 - Affects parallelisation
- **What if you separate the data and instruction memory and buses?**
 - That is called **Harvard Architecture.**
 - Modern commercial systems use a combination of both
 - RAM stores both instruction and data
 - But there are other intermediate memory (**caches**) which are separated for instruction and data



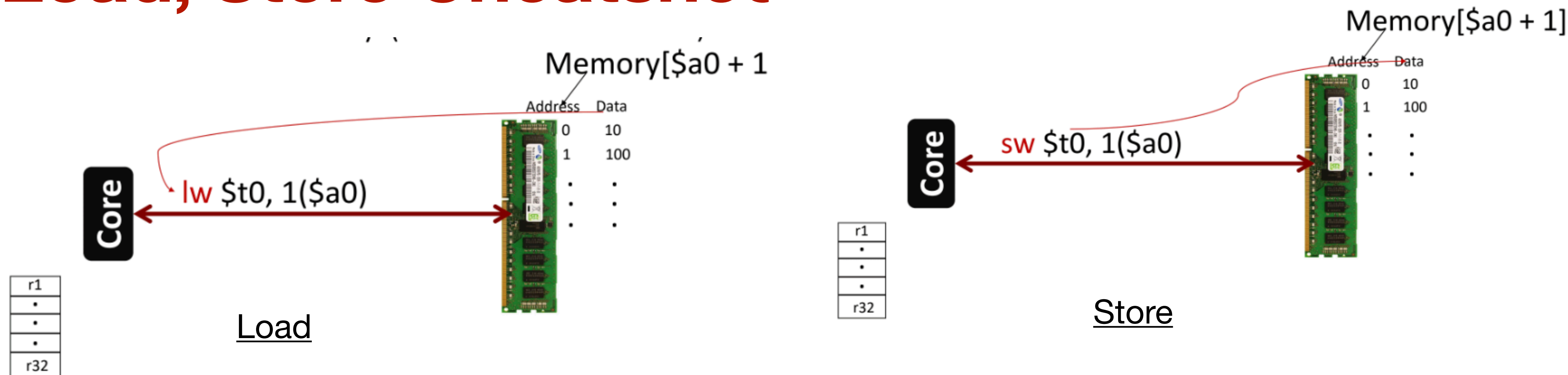
a)



b)

Source: Internet

Load, Store Cheatsheet



Program Counter

Points to the next instruction in the memory to be fetched

```
g = h + A[8];
```

```
PCX: lw $t0, 8($3)      # A[8]
PCY: add $s1, $s2, $t0  # g = h + t0
```

```
PCY = PCX+4
```



Load+Store+Instruction-fetch

Summary...

- Data and instructions at the same place
- Registers are limited — 32 bit wide
- Instructions are 32 bit wide
- Registers are accessed by names
- Memory is accessed by addresses



Decision Making...

- If, else statements in your program...
- How they are interpreted as instructions??

beq (branch equals to) and
bne (branch not equals to)

```
beq $t0, $t1, L1  
bne $t0, $t1, L1
```



Decision Making...

beq \$t0, \$t1, **L1**

goto L1 (statements labeled as L1) if \$t0 equals \$t1

bne \$t0, \$t1, **L1**

goto L1 (statements labeled as L1) if \$t0 does not equal to \$t1



Simple Example...

- Let's compile:

- `if (i == j) f = g + h; else f = g - h;`

Assume:

`$s0` has `i`, `$s1` has `j`, `$s2` has `g`, `$s3` has `h`, `$s4` has `f`

Unconditional Jump

jumps to a specific label

```
beq $s0, $s1, if_equal      # if i == j, jump to if_equal
sub $s4, $s2, $s3            # else: f = g - h
j end_if                    # jump to end
if_equal:
    add $s4, $s2, $s3         # f = g + h
end_if:
```

Decision Making...

- So you can check conditions:
 - `If (x = 0) ..`
 - `If (x != 0) ..`
 - `If (x = y) ..`
 - `If (x != y) ...`
- But how about the following code??

```
if (a < b)
```

```
    c=1
```

```
else
```

```
    c=0
```



Decision Making...

```
if (a < b)
```

```
    c=1
```

```
else
```

```
    c=0
```

- Set on less than (slt)

- `slt $t0, $s3, $s4 # $t0 = 1 if $s3 < $s4`

- `slti $t0,$s2,10 # $t0 = 1 if $s2 < 10`

- After using `slt`, we can use the `beq` or `bne`

Simple Example...

- Let's compile:

- `if (i < j) f = g + h; else f = g - h;`

Assume:

`$s0` has `i`, `$s1` has `j`, `$s2` has `g`, `$s3` has `h`, `$s4` has `f`

<code>slt \$t0, \$s0, \$s1</code>	<code># \$t0 = 1 if i < j</code>
<code>beq \$t0, \$zero, ELSE</code>	<code># if \$t0 == 0, i >= j, jump to ELSE</code>
<code>add \$s4, \$s2, \$s3</code>	<code># f = g + h</code>
<code>j END_IF</code>	<code># jump to END_IF</code>
ELSE:	
<code>sub \$s4, \$s2, \$s3</code>	<code># f = g - h</code>
END_IF:	

Dealing With Loops

- Let's first see how we deal with **arrays**...

- $f = h + A[8]$

Assume:

- $\$t0$ has $A[8]$, $\$s5$ has base address of the array A , $\$s4$ has f , $\$s3$ has h
- Also assume “ $A[8]$ ” as `uint8_t` (a byte)

```
lbu $t0, 8($s5)           # Load word A[8] with byte offset
add $s4, $s3, $t0         # f = h + A[8]
```

- But what is “ $A[8]$ ” is `int` (4 bytes)?????

```
lw $t0, 32($s5)           # Load A[8], 8 * 4 = 32 (word) offset
add $s4, $s3, $t0         # f = h + A[8]
```

Dealing With Loops

- Let's consider:
 - `while (A[i] > k) i = i+1;`

Assume:

`$s0` has `i`,

`$t1` has address of `A[i]`

`$t2` has `A[i]`

`$s6` has `k`

```
LOOP:
sll $t1, $s0, 2           # $s0 = i, i*4 for word offset
add $t1, $s5, $t1         # Compute address A[i]
lw $t2, 0($t1)            # Load A[i] (integer)
slt $t3, $t2, $s6         # $t3 = 1 if A[i] < k
bne $t3, $zero, END_LOOP  # if A[i] < k, exit loop
addi $s0, $s0, 1          # i = i + 1
j LOOP
END_LOOP:
```

Performs left logical shift by two bits..why??

Dealing With Loops

- What happens if:
 - `while (A[i] == k) i = i+1;`

Assume:

`$s0` has `i`,

`$t1` has address of `A[i]`

`$t2` has `A[i]`

`$s6` has `k`

Dealing With Loops

- What happens if:
 - `while (A[i] == k) i = i+1;`

Assume:

`$s0` has `i`,

`$t1` has address of `A[i]`

`$t2` has `A[i]`

`$s6` has `k`

```
LOOP:
    sll $t1, $s0, 2          # $s0 = i, i*4 for word offset
    add $t1, $s5, $t1        # Compute address A[i]
    lw $t2, 0($t1)           # Load A[i] (integer)
    bne $t2, $s6, END_LOOP   # if A[i] != k, exit loop
    addi $s0, $s0, 1         # i = i + 1
    j LOOP
END_LOOP:
```


More on Jumping...

- What happens if:
 - `while (A[i] == k) i = i+1;`

Assume:

`$s0` has `i`,
`$t1` has address of `A[i]`
`$t2` has `A[i]`
`$s6` has `k`

```
LOOP:
    sll $t1, $s0, 2           # $s0 = i, i*4 for word offset
    add $t1, $s5, $t1         # Compute address A[i]
    lw  $t2, 0($t1)           # Load A[i] (integer)
    bne $t2, $s6, END_LOOP    # if A[i] != k, exit loop
    addi $s0, $s0, 1          # i = i + 1
    j  LOOP
END_LOOP:
```



- Normally:
 - `PC, PC+4, PC+8,`
 - But jump instruction loads a new value to the PC
 - It's the offset in the program where the exception should divert (the label is basically that)


More on Jumping...

- What happens if:
 - `while (A[i] == k) i = i+1;`

Assume:

`$s0` has `i`,
`$t1` has address of `A[i]`
`$t2` has `A[i]`
`$s6` has `k`

```
LOOP:  
    sll $t1, $s0, 2  
    add $t1, $s5, $t1  
    lw  $t2, 0($t1)  
    bne $t2, $s6, END_LOOP  
    addi $s0, $s0, 1  
    j  LOOP  
END_LOOP:
```



```
# $s0 = i, i*4 for word offset  
# Compute address A[i]  
# Load A[i] (integer)  
# if A[i] != k, exit loop  
# i = i + 1
```

- Normally:
 - `PC, PC+4, PC+8,`
 - But jump instruction loads a new value to the PC
 - It's the offset in the program where the exception should divert (the label is basically that)
 - But jumping is even more exotic...Let's see why

More on Jumping...

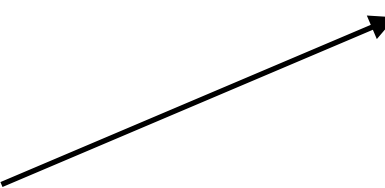


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More on Jumping...Working with Functions

```
int sum(int a, int b)
{
    int c=a+b;
    return c;
}
void main (void)
{
    int i=1;
    int j=2;
    int k = sum(i, j);
    // ...
}
```

Function call
jumps to a
location in
your code



- **Caller:** One who calls the function
- **Callee:** The function which is being called

- **Anatomy of a Function Call:**

- Put parameters in a place where the function can access them.
- Transfer control to the function.
- Acquire the storage resources needed for the function.
- Perform the desired task.
- Put the result value in a place where the caller program can access it.
- Return control to the point of origin, since a function can be called from several points in a program.

Working with Functions — The MIPS Case

- MIPS Support for Function Call:

- `$a0–$a3`: four argument registers in which to pass parameters
- `$v0–$v1`: two value registers in which to return values
- `$ra`: one **return address** register to return to the point of origin

- Ways of Jumping..:

- `jal Label`: Jump and link
- `jr $ra`: Jump back to the return address stored in `$ra`



Working with Functions — The MIPS Case

- **Ways of Jumping..:**
 - `jal Label:`
 - First, save `PC+4` in `$ra`
 - The instruction to be executed next is at `Label`
 - `jr $ra`: Jump back to the return address stored in `$ra`
(`PC + 4`)



Working with Functions — The MIPS Case

Complete Picture

```
int sum(int a)
{
    int c=a+4;
    return c;
}
void main (void)
{
    int i=2;
    int k = sum(i);
}
```

```
sum:
    PC+100: addi $v0, $a0, 4      # c = a + 4, return in $v0
    PC+104: jr $ra               # return to PC+12

main:
    PC+4:  li $a0, 2             # i = 2
    PC+8:  jal sum               # call sum(i); $ra = PC+12
    PC+12: addi $s1, $v0, 0      # k = return value (k = 6)
```